The following exercises will be discussed on July 18th.

Exercise 9-1 Trace Equivalence, Similarity and Bisimilarity

- a) Let us assume that P and Q are doubly similar, i.e. $P \sqsubseteq Q$ and $Q \sqsubseteq P$. Are then P and Q also strongly bisimilar?
- b) Show that P and Q are trace equivalent, if they are strongly bisimilar.

Exercise 9-2

HML Formulas and Labelled Transition Systems

Consider the following LTS:



Prove or disprove the following statements:

- a) $p \vDash [a]\langle b \rangle tt$
- b) $p \models \langle a \rangle \langle b \rangle tt$
- c) $p \vDash [a](\langle a \rangle tt \lor \langle b \rangle tt)$
- d) $p \vDash [a]\langle a \rangle [a][b]ff$
- e) $p \vDash \langle a \rangle \Big([a] \big(\langle a \rangle tt \land [b] ff \big) \land \langle b \rangle ff \Big)$

Exercise 9-3

Bisimulation and HML Formulas

Prove by structural induction over ϕ

$$\forall \phi, \phi \text{ HML formula } \forall s, t \Big(s \sim t \Rightarrow (s \vDash \phi \Leftrightarrow t \vDash \phi) \Big)$$